

# **Graad 11 – Boek B**

(CAPS Uitgawe)

## **INHOUD:**

### **Bladsy:**

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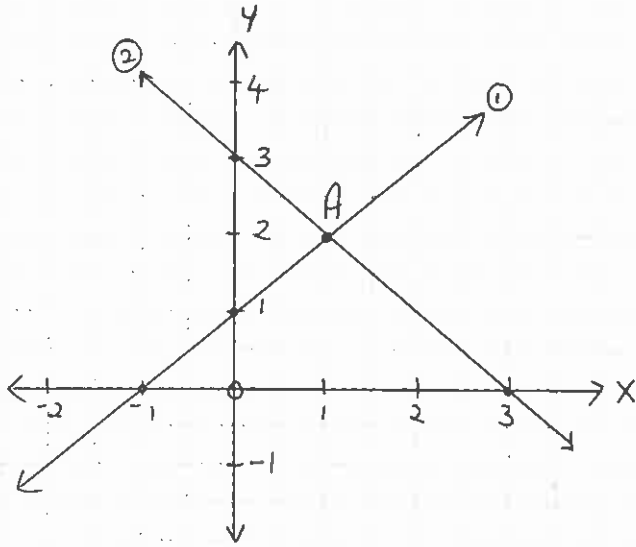
Hierdie boek is opgestel en verwerk deur E.J. Du Toit in 2008.  
Hersiene CAPS uitgawe 2012.

Kontak nommer: 086 618 3709 (Faks!)

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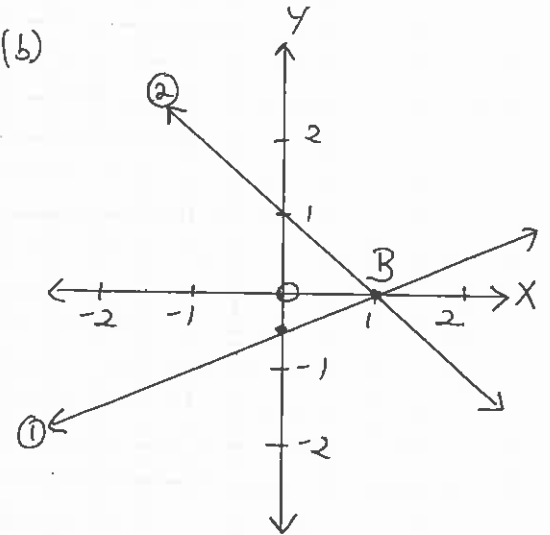
ISBN-13 978-1-919957-65-4

(1)(a)



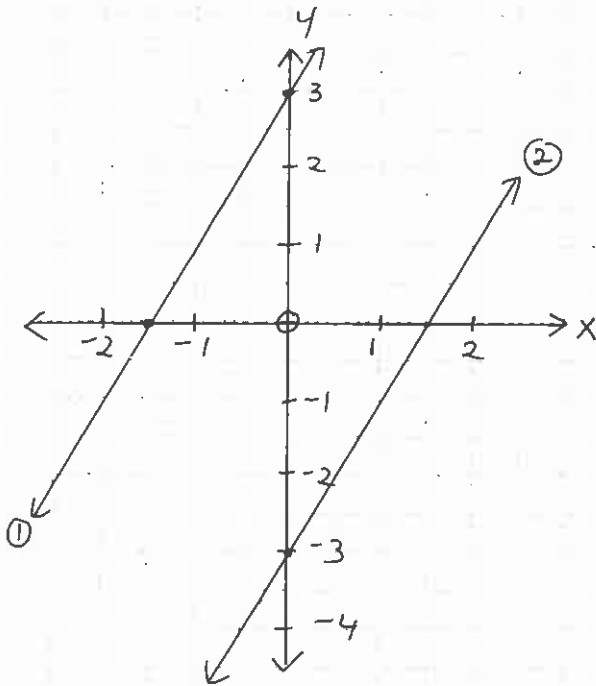
$A(1; 2)$

(b)



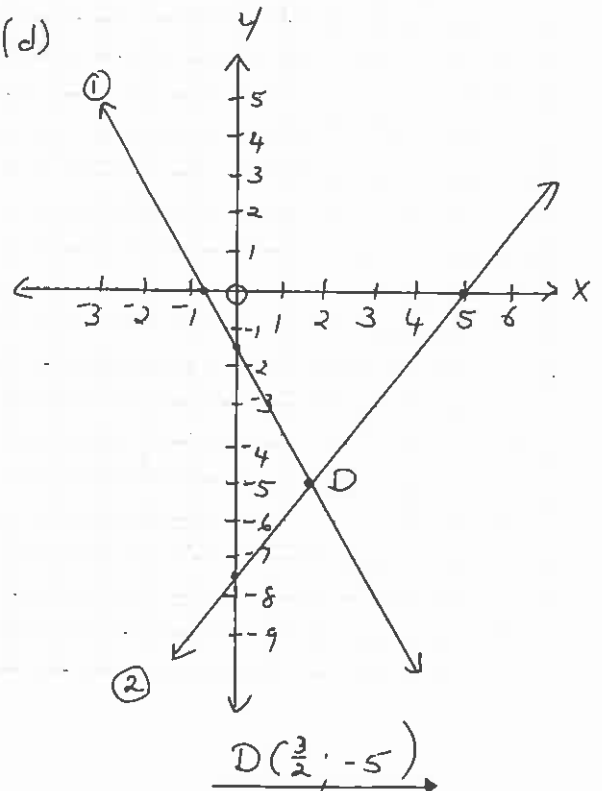
$B(1; 0)$

(c)



Geen snypunt.  
lyne ewewydig!

(d)



$D(\frac{3}{2}; -5)$

# Hoofstuk B1

## Funksies

### B1.1 Lineêre funksie:

Hersiening!

Standaardvorm:  $y = mx + c$  met  $m = \frac{y_2 - y_1}{x_2 - x_1}$  as die gradiënt en  $c$  as die  $y$ -afsnit.

Oefening 1:

Datum: \_\_\_\_\_

(1) Skets die volgende pare reguitlyne telkens op dieselfde assestelsel en bepaal die gemeenskaplike snypunt vir elk:

(a)  $x - y + 1 = 0$  en  $x + y = 3$

$$\begin{aligned} x - y + 1 &= 0 \text{ --- (1)} \\ \underline{x\text{-afsnit: } (-1; 0)} \\ \underline{y\text{-afsnit: } (0; 1)} \\ x + y &= 3 \text{ --- (2)} \\ \underline{x\text{-afsnit: } (3; 0)} \\ \underline{y\text{-afsnit: } (0; 3)} \end{aligned}$$

(b)  $2y + 1 = x$  en  $x + y = 1$

$$\begin{aligned} 2y + 1 &= x \text{ --- (1)} \\ \underline{x\text{-afsnit: } (1; 0)} \\ \underline{y\text{-afsnit: } (0; -\frac{1}{2})} \\ x + y &= 1 \text{ --- (2)} \\ \underline{x\text{-afsnit: } (1; 0)} \\ \underline{y\text{-afsnit: } (0; 1)} \end{aligned}$$

(c)  $2x + 3 = y$  en  $2y - 4x + 6 = 0$

$$\begin{aligned} 2x + 3 &= y \text{ --- (1)} \\ \underline{x\text{-afsnit: } (-\frac{3}{2}; 0)} \\ \underline{y\text{-afsnit: } (0; 3)} \\ 2y - 4x + 6 &= 0 \text{ --- (2)} \\ \underline{x\text{-afsnit: } (\frac{3}{2}; 0)} \\ \underline{y\text{-afsnit: } (0; -3)} \end{aligned}$$

(d)  $4x + 2y = -3$  en  $2y + 15 = 3x$

$$\begin{aligned} 4x + 2y &= -3 \text{ --- (1)} \\ \underline{x\text{-afsnit: } (-\frac{3}{4}; 0)} \\ \underline{y\text{-afsnit: } (0; -\frac{3}{2})} \\ 2y + 15 &= 3x \text{ --- (2)} \\ \underline{x\text{-afsnit: } (5; 0)} \\ \underline{y\text{-afsnit: } (0; -\frac{15}{2})} \end{aligned}$$

(2) Bepaal die vergelyking van die reguitlyn:

(a) deur die punte  $(1; 3)$  en  $(2; -1)$   
 $x_1, y_1$        $x_2, y_2$

$$\begin{aligned} m &= \frac{y_2 - y_1}{x_2 - x_1} = \frac{-1 - 3}{2 - 1} = \frac{-4}{1} = -4 \\ \underline{y - y_1} &= m(x - x_1) \\ \underline{y - 3} &= -4(x - 1) \\ \underline{y - 3} &= -4x + 4 \\ \underline{y} &= \underline{-4x + 7} \end{aligned}$$

(b) deur die punt  $(4; 0)$  en ewewydig  
aan  $3y + 6x - 2 = 0$

$$\begin{aligned} 3y &= -6x + 2 \\ \underline{y} &= \underline{-2x + \frac{2}{3}} \\ \therefore m_1 &= -2 = m_2 \text{ (|| lyn)} \\ \therefore \underline{y - y_1} &= m(x - x_1) \\ \underline{y - 0} &= \underline{-2(x - 4)} \\ \underline{y} &= \underline{-2x + 8} \end{aligned}$$



(c) deur die punte  $(3; -7)$  en  $(3; 4)$

$$x = 3 \text{ in albei punte}$$

$$\therefore x = 3$$

(3) Die punte  $A(3; 5)$ ,  $B(0; 4)$  en  $C(-1; m)$  is kollineêr. Bepaal die waarde van  $m$ .

$$m_{AB} = \frac{4-5}{0-3} = \frac{-1}{-3} = \frac{1}{3}$$

$$m_{BC} = \frac{m-4}{-1-0} = \frac{m-4}{-1}$$

maar vir kollineêr is  $m_{AB} = m_{BC}$

$$\therefore \frac{1}{3} = \frac{m-4}{-1}$$

$$-1 = 3(m-4)$$

$$-1 = 3m - 12$$

$$11 = 3m \quad \therefore m = \frac{11}{3}$$

(d) deur die punt  $(0; 2)$  met 'n inklinasie van  $135^\circ$

$$m = \tan \theta$$

$$m = \tan 135^\circ$$

$$m = -1 \text{ deur } (0; 2)$$

$$\therefore y = mx + c$$

$$y = -1x + 2$$

(4)  $3x - 2y = 3$  en  $px + 1 = 2y$  is loodreg op mekaar. Bereken  $p$ .

$$3x - 2y = 3 \text{ en } px + 1 = 2y$$

$$3x - 3 = 2y \quad y = \frac{p}{2}x + \frac{1}{2}$$

$$\frac{3}{2}x - \frac{3}{2} = y$$

As lyne  $\perp$  is:  $m_1 \times m_2 = -1$

$$\therefore \frac{3}{2} \times \frac{p}{2} = -1$$

$$\frac{3p}{4} = -1$$

$$3p = -4$$

$$p = \frac{-4}{3}$$


## B1.2 Kwadratiese funksie (parabool):

### B1.2.1 Skets van die parabool:


#### B1.2.1.1 Standaardvorm 1:

$$y = ax^2 + bx + c$$

**Invloed van a:** [Vorm!]

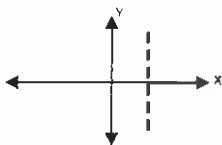
As  $a > 0$ : 

en

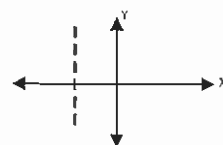
as  $a < 0$ : 

**Invloed van b:** [Simmetrie-as!]

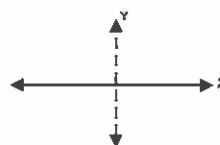
As  $\text{simm-as}(x) = \frac{-b}{2a} > 0$  dan is:



As  $\text{simm-as}(x) = \frac{-b}{2a} < 0$  dan is:



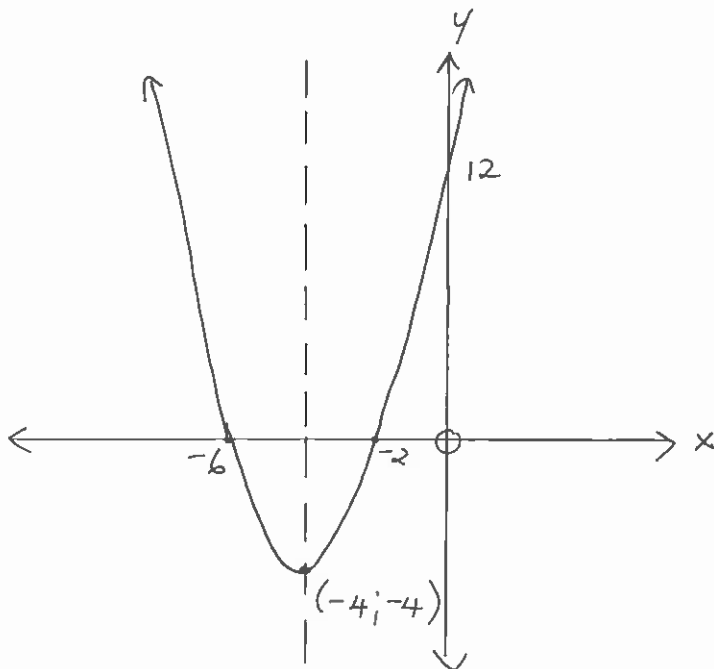
As  $\text{simm-as}(x) = \frac{-b}{2a} = 0$  dan is:



**Invloed van c:** [y-afsnit!]

$c$  verteenwoordig, net soos by die reguitlyn, die  $y$ -afsnit van die parabool.


(1) (a)



Vb. 1 Skets die volgende:  $2y = -2x^2 + 4x + 16$

\*\*\*\*\*

**Stap 1** [Skryf vergelyking in standaardvorm]:  $y = -x^2 + 2x + 8$

**Stap 2** [Interpreteer die vorm]:  $a < 0 \therefore$  

**Stap 3** [Bepaal die y-afsnit]:  $c = 8$  of stel  $x = 0 \therefore$  y-afsnit:  $(0; 8)$

**Stap 4** [Bepaal die x-afsnit(te)]: Daar kan twee, een of geen x-afsnit(te) wees.

$$\text{Stel } y = 0 \rightarrow 0 = -x^2 + 2x + 8$$

$$0 = x^2 - 2x - 8$$

$$0 = (x - 4)(x + 2)$$

$$\therefore x = 4 \text{ of } x = -2$$

$\therefore$  x-afsnitte:  $(4; 0)$  en  $(-2; 0)$

NS: Indien daar nie faktore is nie, maak gebruik van die formule!

**Stap 5** [Bepaal die vergelyking van die simmetrie-as]: Formule  $\rightarrow x = \frac{-b}{2a}$

Uit standaardvorm is  $a = -1$  en  $b = 2 \rightarrow$

$$x = \frac{-2}{2(-1)}$$

$$x = \frac{-2}{-2} = 1$$

of die simm-as is presies tussen die twee x-afsnitte:  $\therefore$  simm-as =  $\frac{4 + (-2)}{2} = \frac{2}{2} = 1$

**Stap 6** [Bepaal die draaipunt se koördinate]:

Vervang  $x = 1$  (simm-as) in vgl van stap 1

$$\therefore y = -x^2 + 2x + 8$$

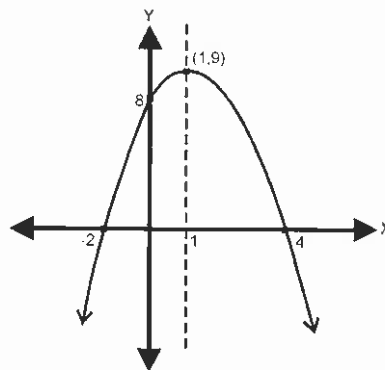
$$\therefore y = -(1)^2 + 2(1) + 8$$

$$\therefore y = -1 + 2 + 8 = 9$$

$$\therefore DP = (1; 9)$$

**Stap 7** [Skets die funksie se kromme]:

Toon x-en y-afsnitte en draaipunt duidelik aan.



**Afleidings:**

Maks waarde van 9

Def vers:  $x \in \mathbb{R}$

Waarde vers:  $y \leq 9$

Datum: \_\_\_\_\_

Oefening 2:

(1) Skets die volgende funksies op verskillende assestelsels: (Skets links!)

(a)  $y = x^2 + 8x + 12$  Vorm:  $a > 0 \curvearrowright$

$$\text{y-afsnit: } (0; 12)$$

$$\text{Simm-as: } x = \frac{-6 + (-2)}{2}$$

$$\text{x-afsnit:}$$

$$x = -4$$

$$0 = x^2 + 8x + 12$$

$$\text{DP: } y = (-4)^2 + 8(-4) + 12$$

$$0 = (x + 6)(x + 2)$$

$$= 16 - 32 + 12$$

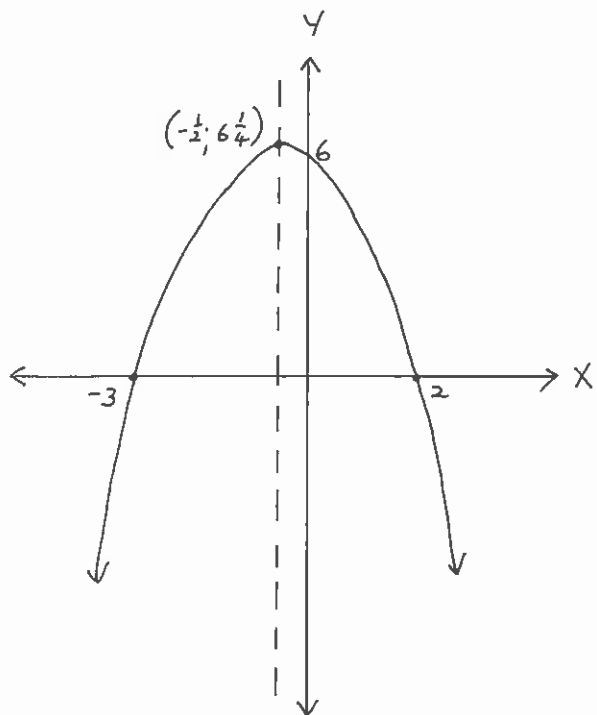
$$\therefore x = -6 \text{ of } x = -2$$

$$y = -4$$

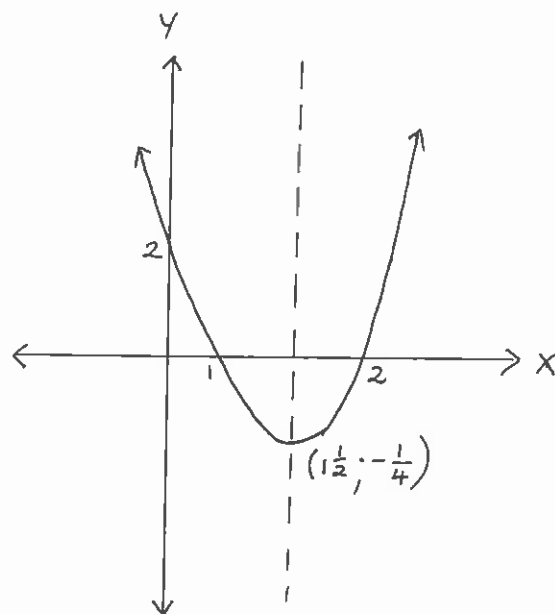
$$(-6; 0) \quad (-2; 0)$$

$$\therefore DP = (-4; -4)$$

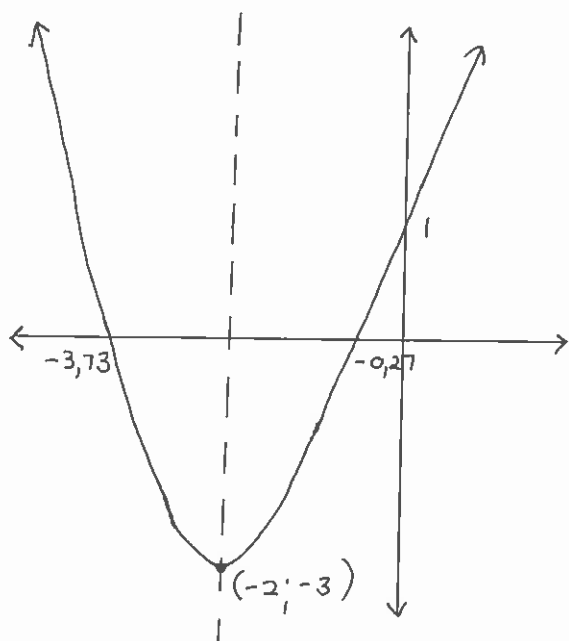
(b)



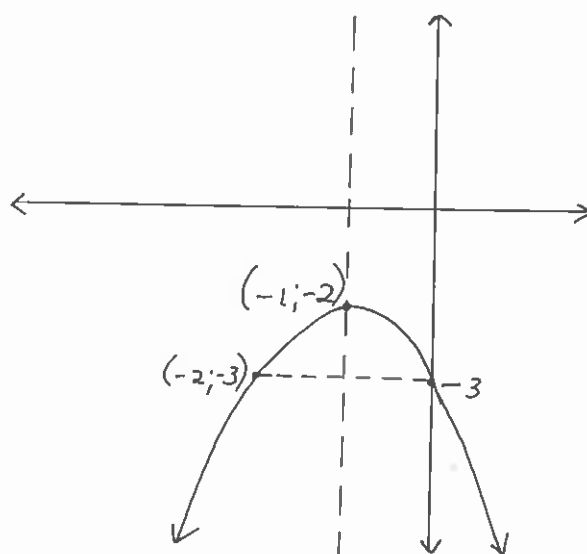
(c)



(d)



(e)





(b)  $y = -x^2 - x + 6$

Vorm:  $a < 0$  ↙

y-afs:  $(0; 6)$

x-afs:  $0 = -x^2 - x + 6$

$0 = x^2 + x - 6$

$0 = (x+3)(x-2)$

$x = -3$  of  $x = 2$

$(-3; 0)$        $(2; 0)$

Simm-GS:  $x = \frac{-b}{2a} = \frac{-(-1)}{2(-1)}$

$\therefore x = -\frac{1}{2}$

DP:  $y = -\left(-\frac{1}{2}\right)^2 - \left(-\frac{1}{2}\right) + 6$

$y = -\left(\frac{1}{4}\right) + \frac{1}{2} + 6$

$y = -\frac{1}{4} + \frac{2}{4} + \frac{24}{4}$

$y = \frac{25}{4}$

$\therefore DP\left(-\frac{1}{2}; \frac{25}{4}\right)$

(c)  $2y = 2x^2 - 6x + 4$

$y = x^2 - 3x + 2$

Vorm:  $a > 0$  ↗

y-afs:  $(0; 2)$

x-afs:  $0 = x^2 - 3x + 2$

$0 = (x-2)(x-1)$

$x = 2$  of  $x = 1$

$(2; 0)$        $(1; 0)$

Simm-GS:  $x = \frac{2+1}{2}$

$\therefore x = \frac{3}{2} = 1\frac{1}{2}$

DP:  $y = \left(\frac{3}{2}\right)^2 - 3\left(\frac{3}{2}\right) + 2$

$y = \frac{9}{4} - \frac{9}{2} + 2$

$y = \frac{9}{4} - \frac{18}{4} + \frac{8}{4}$

$y = -\frac{1}{4}$

$\therefore DP\left(\frac{3}{2}; -\frac{1}{4}\right)$

(d)  $y = x^2 + 4x + 1$

Vorm:  $a > 0$  ↗

y-afs:  $(0; 1)$

x-afs:  $0 = x^2 + 4x + 1$

$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$= \frac{-4 \pm \sqrt{4^2 - 4(1)(1)}}{2(1)}$

$x = \frac{-4 \pm \sqrt{12}}{2}$

$x = -0,27$  of  $x = -3,73$

Simm-GS:  $x = \frac{-b}{2a}$

$x = \frac{-4}{2(1)}$

$x = -2$

DP:  $y = (-2)^2 + 4(-2) + 1$

$= 4 - 8 + 1$

$y = -3$

$\therefore DP(-2; -3)$

(e)  $y = -x^2 - 2x - 3$

Vorm:  $a < 0$  ↙

y-afs:  $(0; -3)$

x-afs:  $0 = -x^2 - 2x - 3$

$0 = x^2 + 2x + 3$

$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$= \frac{-2 \pm \sqrt{(2)^2 - 4(1)(3)}}{2(1)}$

$x = \frac{-2 \pm \sqrt{-8}}{2}$

$\therefore$  Geen  $\mathbb{R}$  wortels

$\Rightarrow$  geen  $x$ -afsnitte

Simm-GS:  $x = \frac{-(-2)}{2(-1)} = -1$

DP:  $y = -(-1)^2 - 2(-1) - 3$

$= -(1) + 2 - 3$

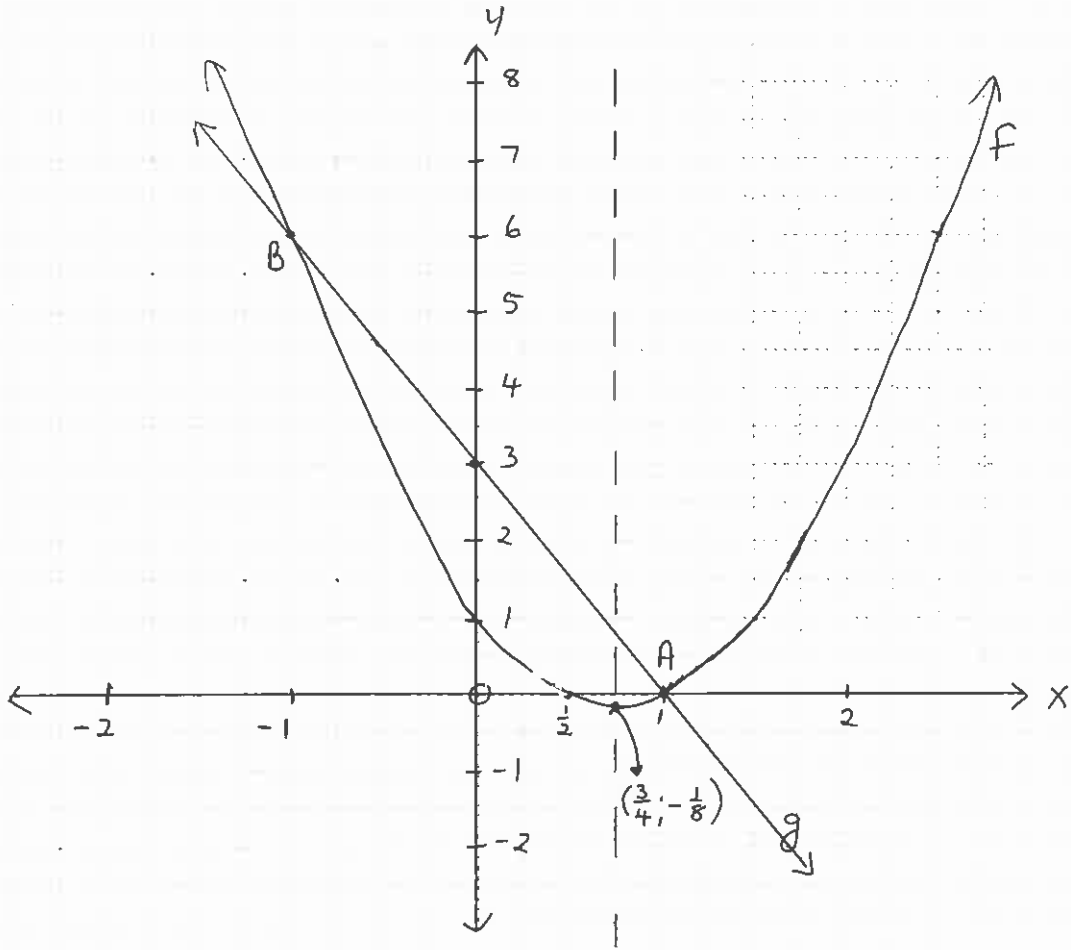
$y = -1 + 2 - 3$

$y = -2$

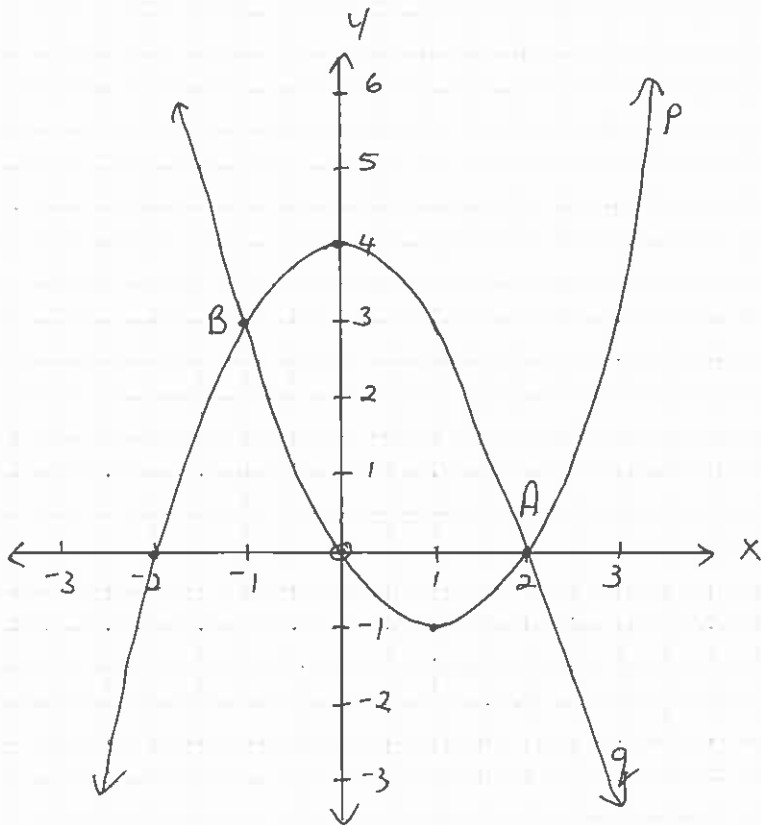
$\therefore DP(-1; -2)$

Kontrolle punt  $P(-2; -3)$

(2)(a)



(3)(a)



(2) Beskou:  $f(x) = 2x^2 - 3x + 1$

(a) Skets f. Toon alle berekeninge.

$$f(x) = y = 2x^2 - 3x + 1 \quad \text{Vorm: } a > 0 \quad \curvearrowright$$

$$\text{y-afs: } (0; 1)$$

$$\text{simmetrie-as: } x = \frac{-b}{2a}$$

$$x\text{-afs: } 0 = 2x^2 - 3x + 1$$

$$x = \frac{-(-3)}{2(2)} = \frac{3}{4}$$

$$0 = (2x-1)(x-1)$$

$$\text{DP: } y = 2\left(\frac{3}{4}\right)^2 - 3\left(\frac{3}{4}\right) + 1$$

$$2x-1=0 \text{ of } x=1$$

$$= 2 \times \frac{9}{16} - \frac{9}{4} + 1$$

$$x = \frac{1}{2}$$

$$y = \frac{9}{8} - \frac{18}{8} + \frac{8}{8}$$

$$y = -\frac{1}{8} \quad \therefore \text{DP} \left(\frac{3}{4}; -\frac{1}{8}\right)$$

(b) Skets op dieselfde assestelsel as in (a):  $g: x \rightarrow -3x + 3$ . Toon alle berekeninge.

$$\therefore y = -3x + 3$$

$$x\text{-afs:}$$

$$y\text{-afs: } (0; 3)$$

$$0 = -3x + 3$$

$$3x = 3 \quad \therefore x = 1 \quad \therefore (1; 0)$$

(c) Bepaal die volgende: (i) g se definisieversameling.

(ii) f se waardeversameling.

(iii) Vergelyking van f se simmetrie-as.

(iv) Die koördinate waar  $f \cap g$ .

$$(i) x \in \mathbb{R}$$

$$(ii) y \geq -\frac{1}{8}$$

$$(iii) x = \frac{3}{4}$$

$$(iv) \text{By } A(1; 0) \text{ en } B(-1; 6)$$

(3) (a) Skets die volgende op dieselfde assestelsel:  $p(x) = x^2 - 2x$  en  $q(x) = 4 - x^2$

$$p(x) = y = x^2 - 2x \quad \curvearrowright$$

$$q(x) = y = 4 - x^2 \quad \curvearrowleft$$

$$y\text{-afs: } (0; 0)$$

$$y\text{-afs: } (0; 4)$$

$$x\text{-afs: } 0 = x^2 - 2x$$

$$x\text{-afs: } 0 = 4 - x^2$$

$$0 = x(x-2)$$

$$0 = (2-x)(2+x)$$

$$x = 0 \text{ of } x = 2$$

$$x = 2 \text{ of } x = -2$$

$$\text{simmetrie-as: } x = \frac{0+2}{2} = 1$$

$$\text{simmetrie-as: } x = \frac{2+(-2)}{2} = 0$$

$$\text{DP: } y = (1)^2 - 2(1)$$

$$\text{DP: } y = 4 - (0)^2$$

$$y = 1 - 2 = -1$$

$$y = 4$$

$$\therefore \text{DP } (1; -1)$$

$$\therefore \text{DP } (0; 4)$$



(b) Bepaal die volgende aan die hand van die grafieke in (a):

(i) Definisieversameling van p.

(iii) Min/Maks waarde van q.

(ii) Waardeversameling van q.

(iv) x as  $p(x) = q(x)$ .

(i)  $D_p: x \in \mathbb{R}$

(iii) Maks. waarde van 4

(ii)  $W_q: y \leq 4$

(iv) By  $A(2; 0)$

en  $B(-1; 3)$

### B1.2.1.2 Standaardvorm 2:

$$y = a(x - p)^2 + q$$

**Invloed van a: [Vorm!]**

As  $a > 0$ :



en

as  $a < 0$ :



**Invloed van p: [Simmetrie-as!]**

Simmetrie-as se vergelyking:  $x = p$

**Invloed van q: [Min/Maks!]**

q verteenwoordig die y-koördinaat van die draaipunt.  $\therefore DP = (p; q)$

Vb. 2 Skets die volgende:

$$y = (x - 1)^2 - 4$$

\*\*\*\*\*

**Stap 1** [Interpreteer die vorm]:  $a > 0$



**Stap 2** [Bepaal die draaipunt se koördinate]:  $DP = (p; q) = (1; -4)$

**Stap 3** [Bepaal x-afsnit(te)]: Stel  $y = 0$

$$\therefore 0 = (x - 1)^2 - 4 \quad \text{of}$$

$$4 = (x - 1)^2$$

$$\pm\sqrt{4} = x - 1$$

$$\pm 2 = x - 1$$

$$\therefore x = +2 + 1 \quad \text{of} \quad x = -2 + 1$$

$$x = 3 \quad \quad \quad x = -1$$

$$0 = (x - 1)^2 - 4$$

$$0 = x^2 - 2x + 1 - 4$$

$$0 = x^2 - 2x - 3$$

$$0 = (x - 3)(x + 1)$$

$$x = 3 \quad \text{of} \quad x = -1$$

$\therefore$  x-afsnitte:  $(3; 0)$  en  $(-1; 0)$

**Stap 4** [Bepaal y-afsnit]: Stel  $x = 0$

$$\therefore y = (0 - 1)^2 - 4$$

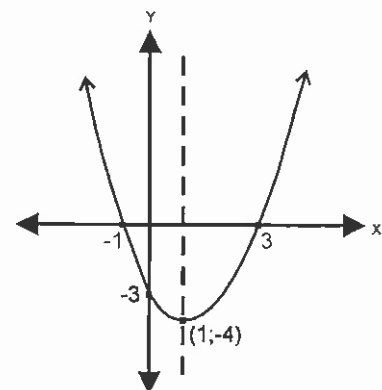
$$\therefore y = (-1)^2 - 4$$

$$\therefore y = 1 - 4$$

$$\therefore y = -3$$

$$\therefore \text{y-afsnit: } (0; -3)$$

**Stap 5** [Teken grafiek!]



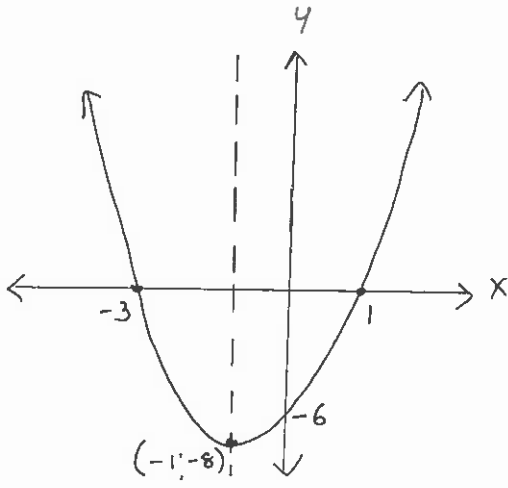
**Afleidings:**

Min waarde van -4

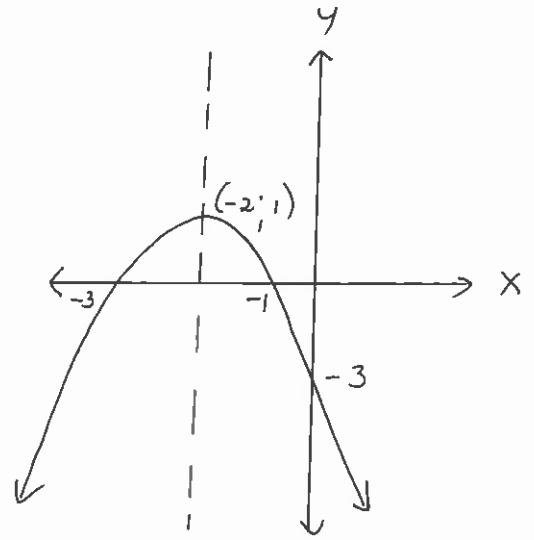
Def vers:  $x \in \mathbb{R}$

Waarde vers:  $y \geq -4$

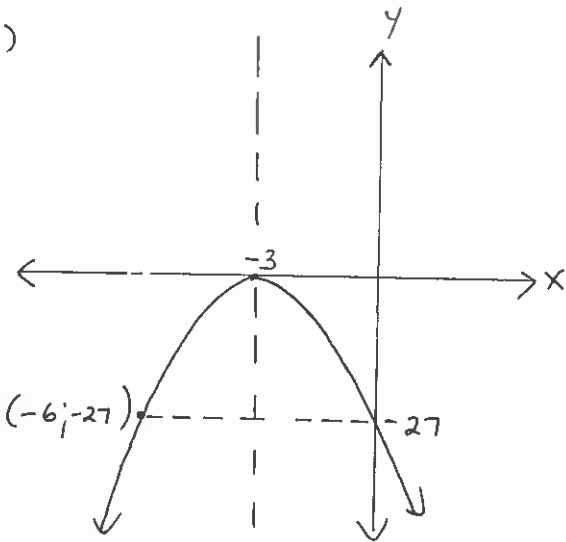
(1)(a)



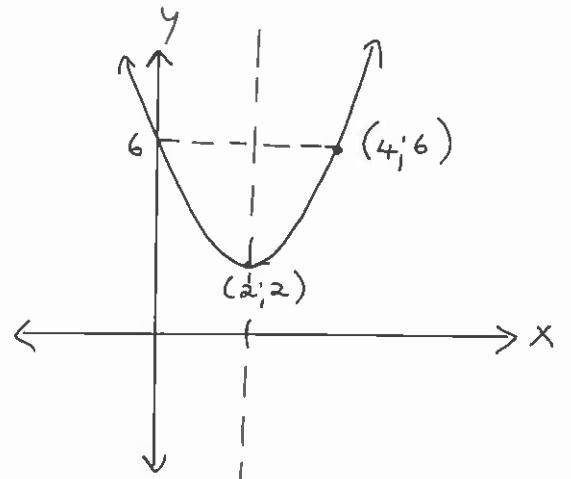
(b)



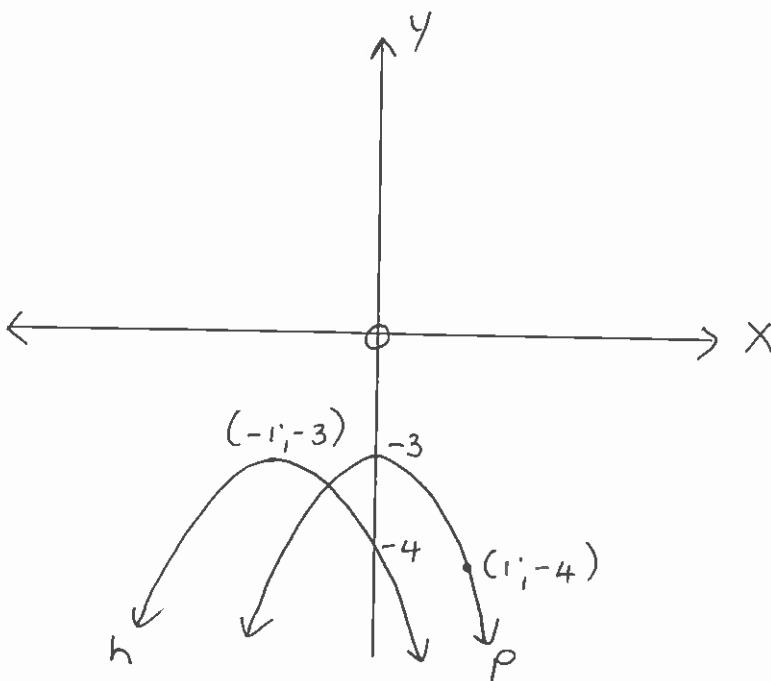
(c)



(d)



(2)



## Oefening 3:

Datum: \_\_\_\_\_

(1) Skets die volgende funksies op verskillende assestelsels: (Skets links!)

(a)  $y = 2(x + 1)^2 - 8$  Vorm:  $\curvearrowright$

DP:  $(-1; -8)$

x-gfs:  $0 = 2(x+1)^2 - 8$

$8 = 2(x+1)^2$

$4 = (x+1)^2$

$\pm 2 = x+1$

$\therefore x = 1$  of  $x = -3$

y-gfs:  $y = 2(0+1)^2 - 8$   
 $= 2(1)^2 - 8$

$y = -6$

(b)  $y = -(x + 2)^2 + 1$  Vorm:  $\curvearrowleft$

DP:  $(-2; 1)$

x-gfs:  $0 = -(x+2)^2 + 1$

$(x+2)^2 = 1$

$x+2 = \pm 1$

$x = -1$  of  $x = -3$

y-gfs:  $y = -(0+2)^2 + 1$

$y = -(2)^2 + 1$

$y = -4 + 1$

$y = -3$

(c)  $y = -3(x + 3)^2$  Vorm:  $\curvearrowleft$

DP:  $(-3; 0)$

x-gfs:  $0 = -3(x+3)^2$

$0 = (x+3)^2$

$\therefore x = -3$  of  $x = -3$

y-gfs:  $y = -3(0+3)^2$

$y = -3(3)^2$

$y = -3(9)$

$y = -27$

(d)  $y = (x - 2)^2 + 2$  Vorm:  $\curvearrowright$

DP:  $(2; 2)$

x-gfs:  $0 = (x-2)^2 + 2$

$-2 = (x-2)^2$

$\pm\sqrt{-2} = x-2$

Geen IR-opl  $\therefore$  geen x-gfs.

y-gfs:  $y = (0-2)^2 + 2$

$= 4 + 2$

$y = 6$

(2) Beskou:  $h: x \rightarrow -(x + 1)^2 - 3$ 

(a) Skets h. Toon alle berekeninge.

Vorm:  $\curvearrowleft$ 

DP:  $(-1; -3)$

x-gfs:  $0 = -(x+1)^2 - 3$

$(x+1)^2 = -3$

$x+1 = \pm\sqrt{-3}$

Geen IR-opl

 $\therefore$  Geen x-gfs.

y-gfs:

$y = -(0+1)^2 - 3$

$y = -(1)^2 - 3$

$y = -1 - 3$

$y = -4$

(b) Skets  $p(x) = -x^2 - 3$  op dieselfde assestelsel as (a).

$\therefore y = -(x+0)^2 - 3$   $\curvearrowleft$

DP:  $(0; -3)$

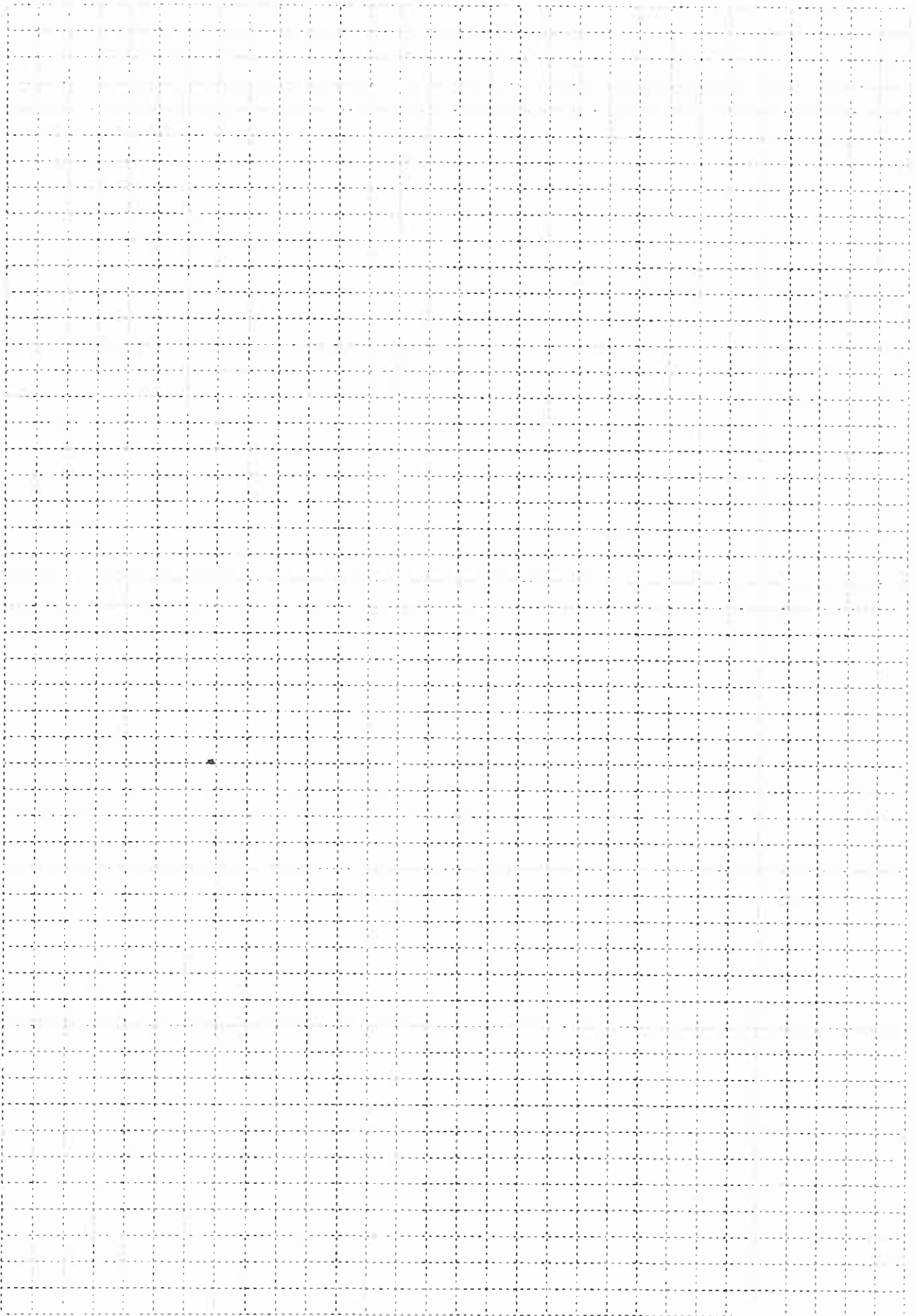
y-gfs:  $(0; -3)$

x-gfs:  $0 = -x^2 - 3$

$x^2 = -3$

$x = \pm\sqrt{-3}$

Geen x-gfs.





- (c) Beskryf die transformasie van h na p soos in die grafiek van (a) en (b). Watter invloed het sodanige transformasie op die vergelykings van h na p:

h skuif 1 eenheid na regs om p te verkry. Die maks. waarde van -3 bly dieselfde, maar simm-as skuif na regs.

- (d) Bepaal die vergelyking van die reguitlyn deur die draaipunte van die twee parabole:

$y = -3$



- (e) Skryf die waardeversamelings van h en p neer:

Wp:  $y \leq -3$     W<sub>h</sub>:  $y \leq -3$

### B1.2.1.3 Standaardvorm 3:

$$y = a(x - x_1)(x - x_2)$$

#### Invloed van a: [Vorm!]


As  $a > 0$ :  en as  $a < 0$ : 

#### Invloed van $x_1$ en $x_2$ : [x-afsnitte!]

Parabool sny x-as by  $x_1$  en  $x_2$ .

Vb. 3 Skets die volgende:  $y = 2(x - 3)(x + 1)$

\*\*\*\*\*

Stap 1 [Interpreteer die vorm]:  $a > 0$   $\therefore$  

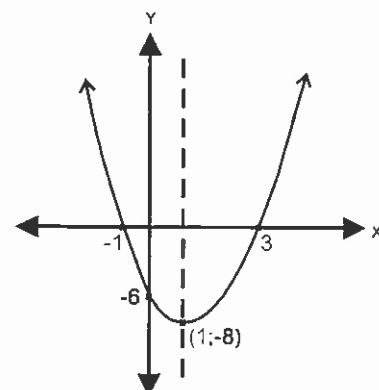
Stap 2 [Bepaal die x-afsnitte]:  $x_1 = 3$  en  $x_2 = -1$   
 $\therefore$  x-afsnitte:  $(3; 0)$  en  $(-1; 0)$

Stap 3 [Bepaal die vergelyking van die simmetrie-as]:  $\text{simm-as} = \frac{x_1 + x_2}{2}$   
 $x = \frac{3 + (-1)}{2} = 1$

Stap 3 [Bepaal die draaipunt se koördinate]:  
 Vervang  $x = 1$  (simm-as) in vergelyking  $\therefore y = 2(1 - 3)(1 + 1)$   
 $\therefore y = 2(-2)(2) = -8$   
 $\therefore$  DP =  $(1; -8)$

Stap 4 [Bepaal y-afsnit]: Stel  $x = 0$   
 $\therefore y = 2(0 - 3)(0 + 1)$   
 $\therefore y = 2(-3)(1)$   
 $\therefore y = -6$   
 $\therefore$  y-afsnit:  $(0; -6)$

Stap 5 [Teken grafiek!]



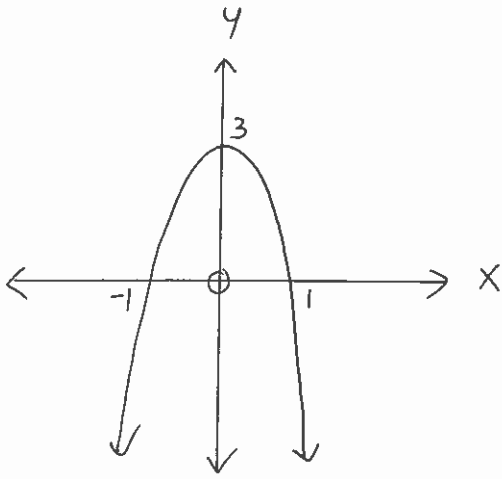
#### Afleidings:

Min waarde van -8

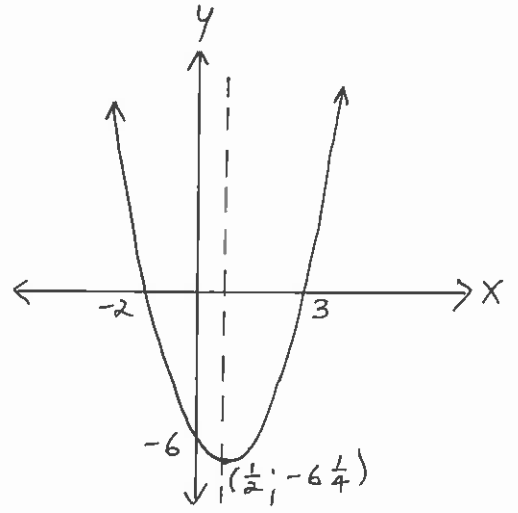
Def vers:  $x \in \mathbb{R}$

Waarde vers:  $y \geq -8$

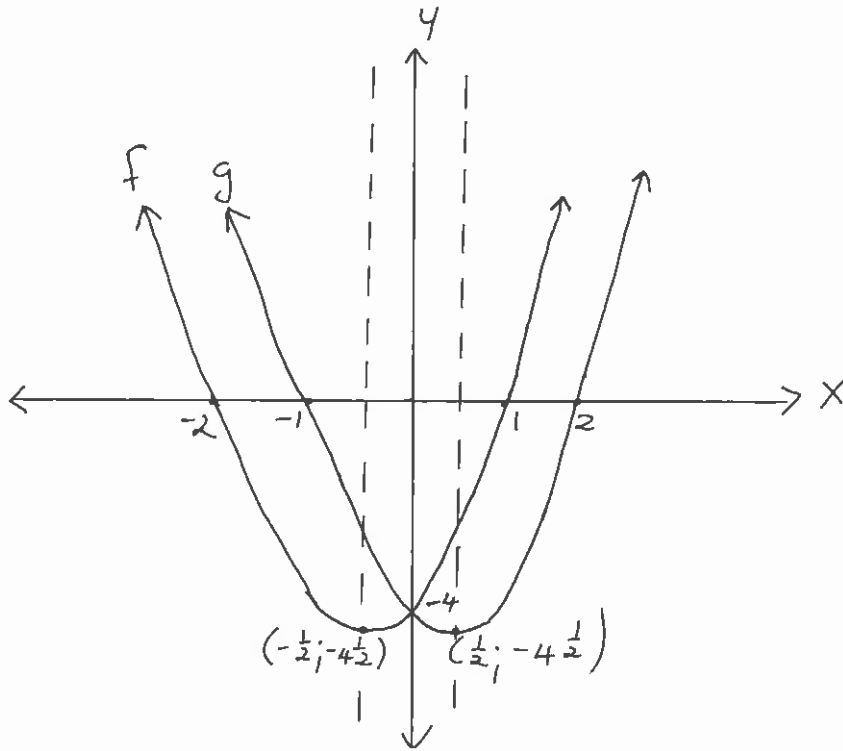
(1)(a)



(b)



(2)



## Oefening 4:

Datum: \_\_\_\_\_

(1) Skets die volgende funksies op verskillende assestelsels: (Skets links!)

(a)  $y = -3(x + 1)(x - 1)$  Vorm:  $\curvearrowright$

x-afs:  $(-1; 0)$   $(1; 0)$

Simm-afs:  $x = \frac{-1+1}{2} = 0$

DP:  $y = -3(0+1)(0-1)$

$y = -3(1)(-1)$

$y = 3$

DP  $(0; 3)$

y-afs:  $y = -3(0+1)(0-1)$

$\therefore y = 3$

(b)  $y = (x + 2)(x - 3)$  Vorm:  $\curvearrowleft$

x-afs:  $(-2; 0)$   $(3; 0)$

Simm-afs:  $x = \frac{-2+3}{2} = \frac{1}{2}$

DP:  $y = (\frac{1}{2}+2)(\frac{1}{2}-3)$

$= (2\frac{1}{2})(-2\frac{1}{2})$

$y = -6\frac{1}{4}$

DP  $(\frac{1}{2}; -6\frac{1}{4})$

y-afs:  $y = (0+2)(0-3)$

$y = (2)(-3)$

$y = -6$

(2) Beskou die volgende:  $f(x) = 2(x - 1)(x + 2)$  en  $g(x) = 2x^2 - 2x - 4$ 

(a) Skets f en g op dieselfde assestelsel.

f: x-afs:  $(1; 0)$   $(-2; 0)$

Simm-afs:  $x = \frac{1-2}{2} = -\frac{1}{2}$

DP:  $y = 2(-\frac{1}{2}-1)(-\frac{1}{2}+2)$

$y = 2(-\frac{3}{2})(\frac{3}{2})$

$y = -4\frac{1}{2}$

$\therefore$  DP  $(-\frac{1}{2}; -4\frac{1}{2})$

y-afs:  $y = 2(0-1)(0+2)$

$y = 2(-1)(2)$

$y = -4$

g: x-afs:  $0 = x^2 - x - 2$

$0 = (x-2)(x+1)$

$x = 2$  of  $x = -1$

Simm-afs:  $x = \frac{2-1}{2} = \frac{1}{2}$

DP:  $y = 2(\frac{1}{2})^2 - 2(\frac{1}{2}) - 4$

$y = -4\frac{1}{2}$

$\therefore$  DP  $(\frac{1}{2}; -4\frac{1}{2})$

y-afs:  $y = 2(0)^2 - 2(0) - 4$

$y = -4$

(b) Skryf g in die vorm  $g(x) = a(x - x_1)(x - x_2)$ 

$g(x) = 2x^2 - 2x - 4$

$g(x) = 2(x^2 - x - 2)$

$g(x) = 2(x-2)(x+1)$

(c) Beskryf die transformasie van  $f \rightarrow g$ . Verduidelik ook die verband tussen die vergelykings van f en g en die transformasie.f is g se refleksie in die y-as.Die vergelykings van f en g is dieselfde behalwe die tekens in die hakies isomgeruil indien in die vorm  $y = a(x - x_1)(x - x_2)$

