

# **Grade 8 – Book C**

**(Revised CAPS edition)**

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This book was drawn up and processed by E.J. Du Toit in 2013.

Contact number: 086 618 3709 (Fax)

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ISBN 978-0-958443-19-7



## Chapter C1

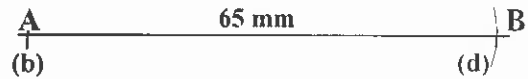
### Construction and measurement

For this chapter you will need a pencil, ruler, protractor and a pair of compasses.

#### **C1.1 Angles and lines:**

##### **C1.1.1 Line segment:**

*E.g.1 Construct  $AB = 65 \text{ mm}$ .*

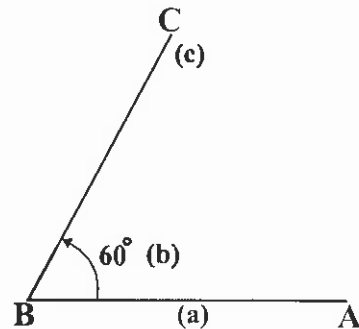


- (a) Draw a long line.
- (b) Mark A.
- (c) Use a compass and measure 65 mm on your ruler.
- (d) Place the compass on A and make a mark on B, 65 mm from .

##### **C1.1.2 Angles:**

*E.g.2 Construct  $\hat{ABC} = 60^\circ$ .*

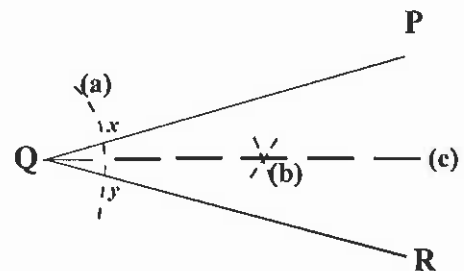
- (a) Draw line AB.
- (b) Place the protractor with "centre" on B.
- (c) Mark C at  $60^\circ$ .
- (d) Join B and C.



##### **C1.1.3 Bisecting an angle:**

*E.g.3 Bisect  $\hat{PQR}$ .*

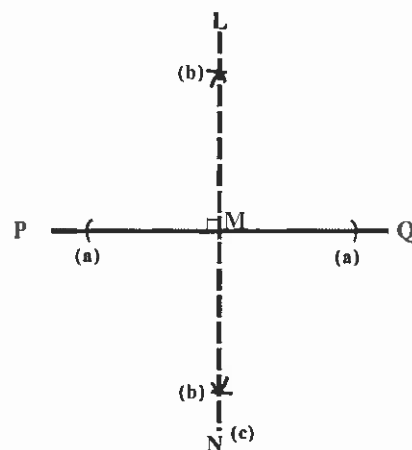
- (a) Place the compass on Q and make a little arch that intersects PQ and QR.
- (b) Alternately place the compass on x and y and make a crossbow.
- (c) Join Q with the intersection of the crossbow.



##### **C1.1.4 Perpendicular line:**

*E.g.4 Construct a perpendicular line through M.*

- (a) Place the compass on M and make arches on both sides of M.
- (b) Then place the compass on both (a)'s on both sides of M and make crossbows on either sides of PMQ so that it intersects the arches in (b).
- (c) Join the intersections of the arches.
- (d)  $\therefore LN \perp PMQ$ , which means  $\hat{PML} = 90^\circ$ .

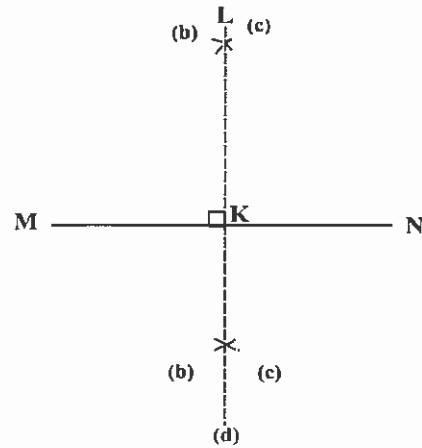




### C1.1.5 Perpendicular bisector:

E.g.5 Construct the perpendicular bisector of MN.

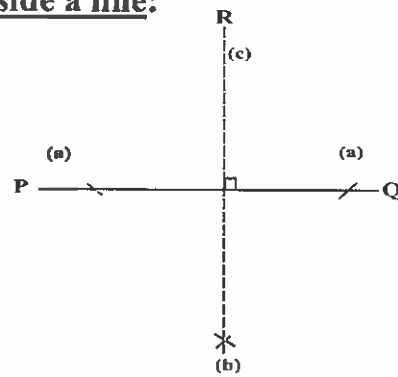
- Open the compass on more than half the length of MN.
- Place the compass on M and make arches on both sides of MN.
- Then place the compass on N and make cross-bows on either sides of MN so that it intersects the arches in (b).
- Join the intersections of the arches.
- $\therefore MK = KN$  and  $KL \perp MN$ , which means  $\hat{MKL} = 90^\circ$ .



### C1.1.6 Draw a perpendicular line from a point outside a line:

E.g.6 Draw the perpendicular line from R on PQ.

- Place the compass on R and make arches on PQ on either sides of R.
- Place the compass alternately on the arches made in (a) and make a crossbow on the other side of PQ.
- Join R with (b).



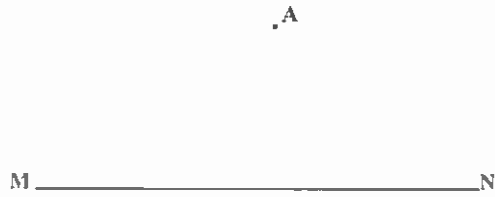
Exercise 1:

Date: \_\_\_\_\_

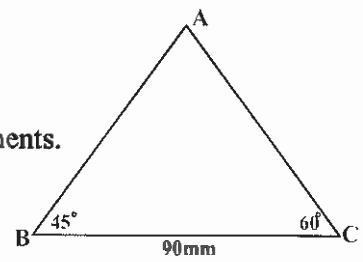
- Construct a line  $AB = 45 \text{ mm}$ .
  - Then construct  $\hat{ABC} = 45^\circ$ .
  
- Construct a line  $MN = 60 \text{ mm}$ .
  - Construct the perpendicular bisector of MN.
  
- Construct a line  $PQ = 72 \text{ mm}$ .
  - Construct  $\hat{RQP} = 60^\circ$ .
  - Bisect  $\hat{RQP}$ .



(4) Construct a perpendicular line on MN from point A.



(5) Construct the following triangle according to the given measurements.  
(This triangle is not drawn to scale!)



☺ Construct  $RS \parallel PQ$  with  $RS \perp AB$  and  $PQ \perp AB$ .

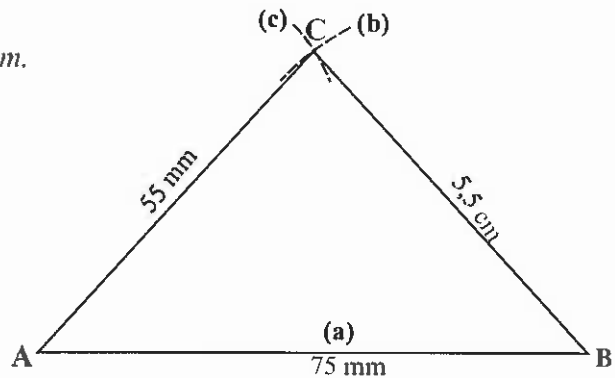




## C1.2 Triangles:

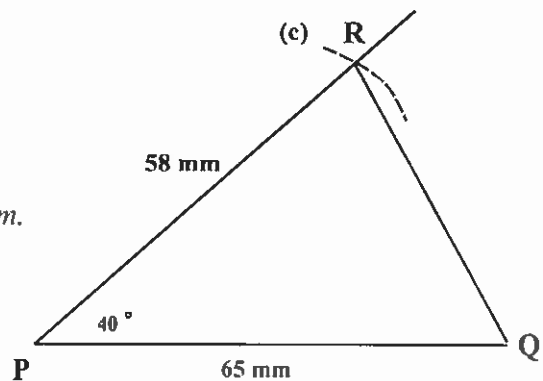
E.g.7 Construct  $\triangle ABC$  with:  $AB = 75 \text{ mm}$ ;  $BC = 5,5 \text{ cm}$  and  $AC = 55 \text{ mm}$ .

- Draw line  $AB = 75 \text{ mm}$ .
- Use a compass, measure  $5,5 \text{ cm} = 55 \text{ mm}$  on a ruler and place compass on  $B$ . Make an arch.
- With compass, measure  $55 \text{ mm}$  on ruler and place compass on  $A$ . Make an arch which intersects the arch in (b).
- Point  $C$  is where (b) intersects (c).



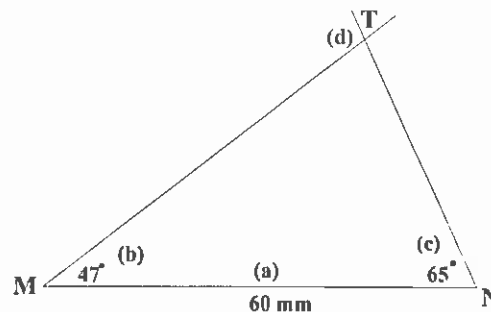
E.g.8 Construct  $\triangle PQR$  with:  $PQ = 6,5 \text{ cm}$ ;  $PR = 5,8 \text{ cm}$  and  $\hat{P} = 40^\circ$ .

- Draw a line  $PQ = 65 \text{ mm}$ .
- Construct  $\hat{P} = 40^\circ$  with your protractor.
- Use a compass and a ruler and measure  $58 \text{ mm}$ . Place compass on  $P$ , tick  $58 \text{ mm}$  on new line.
- $R$  is where (c) intersects the new line. Join  $RQ$ .



E.g.9 Construct  $\triangle MNT$  with:  $\hat{M} = 47^\circ$ ;  $\hat{N} = 65^\circ$  and  $MN = 0,06 \text{ m}$ .

- Draw line  $MN = 0,06 \text{ m} = 6 \text{ cm} = 60 \text{ mm}$ .
- Construct  $M = 47^\circ$  by using a protractor.
- Construct  $N = 65^\circ$  by using a protractor.
- $T$  is where (b) intersects (c).



### Exercise 2:

Date: \_\_\_\_\_

- Construct  $\triangle ABC$  with  $AB = 80 \text{ mm}$ ;  $BC = 66 \text{ mm}$  and  $AC = 4 \text{ cm}$ .
  - Construct the perpendicular bisector of  $AB$ .



- (2) (a) Construct  $\triangle ABC$  with  $\hat{A} = 90^\circ$ ,  $AB = 60$  mm and  $AC = 44$  mm.  
(b) Bisect  $\hat{ABC}$ .

- (3) (a) Construct  $\triangle PQR$  with  $\hat{P} = 35^\circ$ ,  $\hat{R} = 70^\circ$  and  $PR = 7$  cm.  
(b) Construct the perpendicular line from R on PQ.

- ☺ (a) Construct triangle ABC with  $AB = AC = 60$  mm and  $BC = 80$  mm.  
(b) Construct the altitude from triangle ABC passing through point A.  
(c) Which type of triangle is  $\triangle ABC$ ? \_\_\_\_\_

### C1.3 Regular polygons:

E.g.10 Construct a regular hexagon.

(a) Determine the size of each segment:

$$\frac{360^\circ}{6} = 60^\circ$$

(b) Draw any circle.

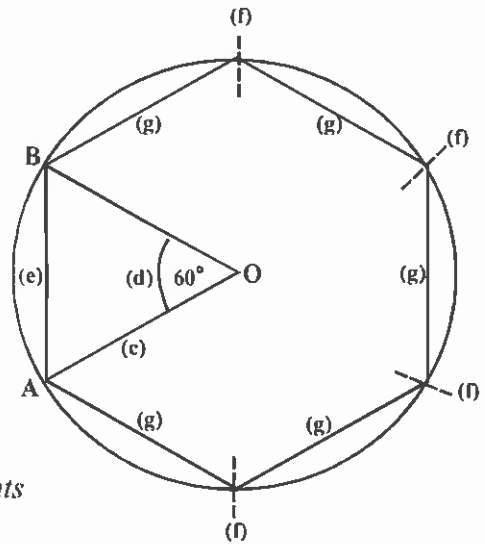
(c) Mark the midpoint with an  $O$  and draw  $OA$ .

(d) From  $OA$ , at  $O$ , construct  $\hat{A}OB = 60^\circ$ .

(e) Join  $AB$ . Use a compass and measure the length of  $AB$ .

(f) Use the length of  $AB$ , measured in (e) on a compass, and from  $B$ , mark another five line segments of the same size on the perimeter of the circle.

(g) Join the points in (f).



Exercise 3:

Date: \_\_\_\_\_

(1) Construct a regular octagon.

(2) Construct a regular pentagon.

☺ With a regular polygon, the size of the angle at centre of each segment is  $30^\circ$ .

How many sides does the polygon have? \_\_\_\_\_

\_\_\_\_\_

**C1.4 Constructions without protractors:**

Exercise 4:

Date: \_\_\_\_\_

(1) (a) Construct  $\hat{PQR} = 90^\circ$ .(b) Use (a) and construct  $\hat{PQS} = 45^\circ$ , without using a protractor.(2) (a) Construct  $\triangle ABC$  with  $AB = BC = AC = 7$  cm.(b) Measure the size of  $\hat{A}$ ,  $\hat{B}$  and  $\hat{C}$  in  $\triangle ABC$ .

(c) Which type of triangle is ABC? \_\_\_\_\_

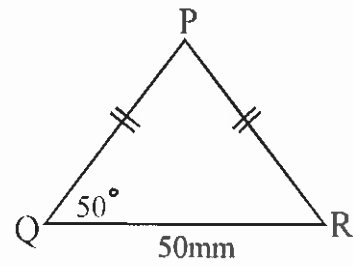
(d) Use (a) and construct  $\hat{ABD} = 30^\circ$ , without using a protractor.(3) (a) Construct  $\hat{TRS} = 90^\circ$ .(b) Use (a) and construct  $\hat{PRS} = 135^\circ$ , without using a protractor.



**C1.5 REVISION EXERCISE:**

Date: \_\_\_\_\_

(1) Construct the following figure according to the given scale.

(2) (a) Construct  $\triangle MNS$  as follows:

$MN = 7 \text{ cm}$  ,  $NS = 8 \text{ cm}$  and  $MS = 70 \text{ mm}$ .

(b) Construct the perpendicular bisector of NS with B as midpoint, on NS.

Extend the perpendicular bisector. This should pass through M!

(c) What will the estimated length of MB be?

(d) Check your answer in (c) by:

(i) using the theorem of Pythagoras.

(ii) measuring the line in the construction with a ruler.

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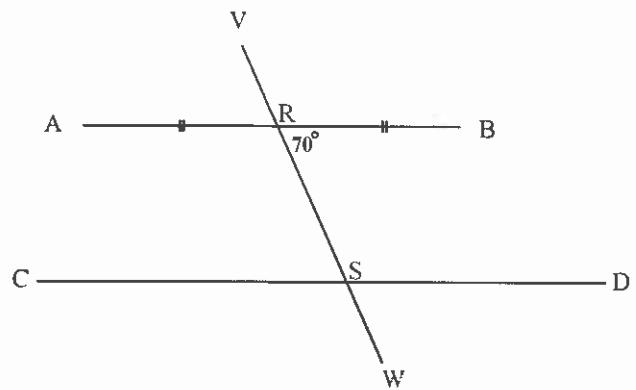




- (3) (a) Construct a circle with radius 4 cm.  
 (b) Construct a regular quadrilateral.  
 (c) What type of quadrilateral is this?
- 

- (4) Construct the following figure according to the given measurements:

- AB = 80 mm
- AR = RB
- RS = 35 mm
- CD = 0,12 m
- $\hat{D}SW = \hat{B}RS = 70^\circ$
- VR = SW = 1 cm
- CS = 2 SD



- (5) (a) Construct equilateral  $\triangle KLT$ .  
 (b) Use (a) and construct  $\hat{K}TS = 120^\circ$ , without using a protractor.

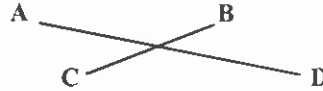


## Chapter C2

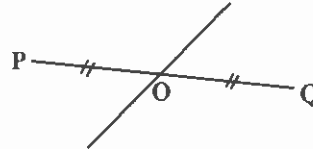
### Lines and angles

#### C2.1 Lines:

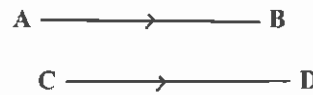
- (1) Secants: Two lines intersecting  
 $\therefore$  AD intersects BC.



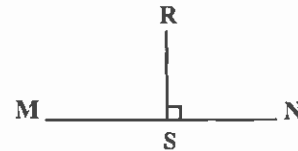
- (2) Bisector: One line intersects another exactly in the middle.  
 $\therefore$  PO = OQ.



- (3) Parallel lines: Two or more lines which are always the same distance apart and will never cross each other.  
 $\therefore$  AB // CD.









- (4) Perpendicular lines: A line is perpendicular to another line if it makes a  $90^\circ$  angle with the other line.  
 $\therefore$  RS  $\perp$  MN.



#### C2.2 Angles:

- (1) Types of angles:

Name of angle:	Example:	Size of angle:
Acute angle		Greater than $0^\circ$ but smaller than $90^\circ$ .
Right angle		Equal to $90^\circ$ .
Obtuse angle		Greater than $90^\circ$ but smaller than $180^\circ$ .
Straight angle		Equal to $180^\circ$ .
Reflex angle		Greater than $180^\circ$ but smaller than $360^\circ$ .
Revolution		Equal to $360^\circ$ .

- (2) Adjacent angles:

Two angles with a common vertex and a common arm and the two angles lie on either side of the common arm.

