# $\frac{Grade\ 10-Book\ A}{(Revised\ edition-CAPS)}$

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## Chapter A1

#### **Number systems**

#### NO CALCULATOR MAY BE USED IN THIS CHAPTER!

#### A1.1 Number systems:

Exercise 1:

Date:

Complete:

- \* Natural numbers:
- $\mathbb{N}$
- = {\_\_\_\_\_}
- \* Whole numbers:
- $\mathbb{N}_0 = \{\underline{\hspace{1cm}}\}$
- \* Integers:

- \* Rational numbers:
- = {\_\_\_\_\_}  $\mathbb{O}$

# **A1.2 Rational numbers:**

#### A1.2.1 Equivalent fractions:

**E.g.1** Write down two equivalent fractions for  $\frac{2}{3}$ :

$$\frac{2\times3}{3\times3} = \frac{6}{9}$$

$$\frac{2 \times 3}{3 \times 3} = \frac{6}{9}$$
 or  $\frac{2 \times 5}{3 \times 5} = \frac{10}{15}$ 

Exercise 2:

Date:

- (1) Write down three equivalent fractions for each of the following rational numbers:
  - (a)  $\frac{-1}{4} = \underline{\hspace{1cm}} = \underline$

  - (c)  $\frac{1}{6} = \underline{\hspace{1cm}} = \underline{$

  - (e)  $\frac{12}{14} = \underline{\hspace{1cm}} =$
  - $2\frac{6}{11} = \underline{\hspace{1cm}} = \underline{\hspace{1cm}}$ (g)
- (2) Are the following equivalent fractions or not? (Answer yes or no only.)
- (a)  $\frac{12}{5} = \frac{24}{10}$ ?: \_\_\_\_ (b)  $\frac{7}{3} = \frac{3}{7}$ ?: \_\_\_\_ (c)  $\frac{3}{-2} = \frac{6}{4}$ ?: \_\_\_\_
- (d)  $\frac{3}{-5} = \frac{-9}{15}$ ?: \_\_\_\_ (e)  $\frac{2}{3} = \frac{4}{9}$ ?: \_\_\_\_ (f)  $\frac{3}{1} = \frac{48}{16}$ ?: \_\_\_\_
- (g)  $\frac{4}{3} = \frac{-12}{-9}$ ?: \_\_\_\_ (h)  $\frac{25}{10} = \frac{5}{2}$ ?: \_\_\_\_ (i)  $\frac{5}{4} = \frac{4}{3}$ ?: \_\_\_\_

#### A1.2.2 Order of rational numbers:

**E.g.2** (a) Arrange the following fractions in ascending order:  $\frac{1}{2}$ ;  $\frac{3}{4}$  and  $\frac{2}{3}$ :

$$\frac{1}{2} = \frac{6}{12}$$

$$\frac{1}{2} = \frac{6}{12}$$
 ;  $\frac{3}{4} = \frac{9}{12}$  and  $\frac{2}{3} = \frac{8}{12}$ 

$$\frac{2}{3} = \frac{8}{12}$$

$$\therefore \frac{1}{2} < \frac{2}{3} < \frac{3}{4}$$

(b) Write down a rational number between  $\frac{3}{4}$  and  $\frac{1}{3}$ :

$$\frac{3}{4} = \frac{9}{12}$$
 and  $\frac{1}{3} = \frac{4}{12}$ 

$$\frac{1}{3} = \frac{4}{12}$$

 $\therefore \frac{1}{2} < \frac{5}{12} \text{ or } \frac{6}{12} \text{ or } \frac{7}{12} \text{ or } \frac{8}{12} < \frac{3}{4}$ 

Exercise 3:

Date:

- (1) Arrange the following fractions in ascending order:
  - (a)  $\frac{3}{4}$ ;  $\frac{2}{3}$  and  $\frac{4}{5}$ :
  - (b)  $\frac{2}{3}$ ;  $\frac{5}{7}$  and  $\frac{4}{6}$ :
- (2) Arrange the following fractions in descending order:
  - (a)  $\frac{5}{6}$ ;  $\frac{2}{3}$  and  $\frac{3}{4}$ :
  - (b)  $-1\frac{1}{2}$ ;  $-1\frac{2}{3}$  and  $\frac{-7}{5}$ :
- (3) Place a rational number between each of the following numbers:
  - (a)  $\frac{-1}{3}$  and  $\frac{-3}{5}$ :
  - (b)  $\frac{3}{4}$  and  $\frac{7}{10}$ :

#### **A1.2.3** Conversion of common fractions to decimal fractions:

E.g.3 Express the following as decimal fractions, without using a calculator:

(a) 
$$\frac{3}{8} = \frac{3,000...}{8} = \frac{3,306040}{8} = 0,375$$

(a) 
$$\frac{3}{8} = \frac{3,000...}{8} = \frac{3,306040}{8} = 0,375$$
 (b)  $1\frac{2}{3} = 1\frac{2,000...}{3} = 1\frac{2,202020...}{3} = 1,66... = 1,6$ 

_			•	4
Ex	01	01	100	/1
1 '. X	C1		7	4

Express the following as decimal fractions, without using a calculator:

(1) 
$$\frac{22}{7} =$$

(2) 
$$4\frac{2}{3} =$$

(3) 
$$\frac{1}{8} =$$

$$(4) \quad \frac{7}{9} =$$
\_\_\_\_\_\_

$$(5) \quad \frac{17}{25} =$$

(6) 
$$\frac{5}{100} =$$

$$(7) \quad \frac{4}{11} = \underline{\hspace{1cm}}$$

(8) 
$$-2\frac{6}{7} =$$
\_\_\_\_\_

(9) 
$$-5\frac{5}{6} =$$
\_\_\_\_\_

$$(10) \quad \frac{33}{8} =$$

#### A1.2.4 Rounding off decimal fractions:

E.g.4 Round off the following fractions correct to the number of decimals indicated in brackets:

(a) 4,34712 (to 3 dec)

(b) 290, 09832 (to 2 dec)

= 4,34712

= 290,09832 **Consider the underlined number** 

≈ **4.347** 

 $\approx 290.10$ 

Exercise 5:

Date:

- (1) Round off the following fractions correct to the number of decimals indicated in brackets:
  - (a) 3,573 (to 2 dec)

(b) 12,00873 (to 3 dec)

(c) 0,00384 (to 5 dec)

(d) 7,3226 (to 1 dec)

(e) 8,39999 (to 1 dec)

(f) 90,9023 (to the nearest integer)

(g) 0,433218 (to 4 dec)

(h) 1 456,6799 (to 3 dec)

(i) 13,00034 (to 3 dec)

(i) 66,666 (to 2 dec)

- (2) Consider the following and choose the correct way of rounding off in brackets:
  - (a)  $3,47653 \approx 3,477$  correct to the nearest (tenth, hundredth or thousandth)
  - (b) 96 995,31956  $\approx$  96 995,32 correct to the nearest (tenth, hundredth or thousandth)

#### A1.2.5 Conversion of decimal fractions to common fractions:

E.g.5 Express the following as common fractions in its simplest form:

(a) 
$$4, 5 = 4\frac{5}{10} \left( \div \frac{5}{5} \right) = 4\frac{1}{2}$$

(b) 
$$-0, 12 = -\frac{12}{100} \left( \div \frac{4}{4} \right) = -\frac{3}{25}$$

Exercise 6:

(9)

Date: \_\_\_\_\_

Express the following as common fractions in its simplest form:

\_\_\_\_\_

$$(4) \quad -0.5 =$$

\_\_\_\_\_

$$(5)$$
  $-1,2 =$ 

\_\_\_\_\_

\_\_\_\_\_

100,75 = \_\_\_\_\_

## **A1.2.6** Conversion of recurring fractions to common fractions:

E.g.6 Convert the following to common fraction in its simplest form:

(a) 
$$0, \dot{1} = \frac{1}{9}$$
 ;  $0, \dot{3} = \frac{3}{9} = \frac{1}{3}$  ;  $0, \dot{5} = \frac{5}{9}$  ;  $0, \dot{8} = \frac{8}{9}$ 

(b) 
$$3,\dot{2}\dot{4}=3\frac{24}{99}=3\frac{8}{33}$$
 ;  $0,\dot{4}\dot{2}\dot{1}=\frac{421}{999}$  ;  $15,\dot{1}\dot{6}\dot{5}\dot{3}=15\frac{1653}{9999}=15\frac{551}{3333}$ 

(c) 
$$0,0\dot{3} = 0,\dot{3} \div 10 = \frac{3}{9} \div \frac{10}{1} = \frac{3}{9} \times \frac{1}{10} = \frac{3}{90} = \frac{1}{30}$$

(d) 
$$0,00\dot{4}\dot{6} = 0,\dot{4}\dot{6} \div 100 = \frac{46}{99} \div \frac{100}{1} = \frac{46}{99} \times \frac{1}{100} = \frac{46}{9900} = \frac{23}{4950}$$

(e) 
$$\mathbf{0}, \mathbf{57} = \mathbf{0}, \mathbf{5} + \mathbf{0}, \mathbf{07} = \mathbf{0}, \mathbf{5} + \mathbf{0}, \dot{\mathbf{7}} \div \mathbf{10} = \frac{5}{10} + \frac{7}{9} \times \frac{1}{10} = \frac{5 \times 9}{10 \times 9} + \frac{7}{90} = \frac{45 + 7}{90} = \frac{52}{90} = \frac{26}{45}$$

Exer	<u>cise 7</u> :		Date:
Conv	vert the following to common fraction	ns in its simples	t form: (Without a calculator.)
(1)	3, Ġ	(2)	0, 13
		-	
_		-	
(3)	22,39	(4)	$-1,\dot{1}\dot{3}\dot{5}$ or $-1,\overline{135}$
_			
_		- -	
_			
(5)	0,7	(6)	0,003
		- -	
		· - · -	
_		 	
(7)	$1,\overline{214}$	(8)	3,258
		-	

☺	Calculate the following without using a calculator: $0, \dot{4} + \frac{2}{3}$
	<u></u>
	·
	·

#### A1.3 Irrational and Real numbers:

Irrational numbers cannot be expressed as a ratio between two integers. These numbers are non-terminating and non-recurring decimals.

E.g. 7 Irrational numbers:

- $\sqrt{2}$  or  $\sqrt{7}$  or  $\sqrt{\frac{3}{4}}$  etc. because 2; 7 and 3 are not perfect squares!
- $\sqrt[3]{12}$  or  $\sqrt[3]{100}$  etc. because 12 and 100 are not perfect cubes!

Whereas the following numbers are rational numbers:

- $\sqrt{4}$  or  $\sqrt{0,01}$  or  $\sqrt{\frac{25}{9}}$  etc. because 4; 0,01; 25 and 9 are perfect squares!
- $\sqrt[3]{27}$  or  $\sqrt[3]{125}$  etc. because 27 and 125 are perfect cubes!

The real numbers,  $\mathbb R$  consist of the rational numbers,  $\mathbb Q$  and the irrational numbers,  $\mathbb Q'$ . Remember that all terminating and recurring decimals are rational numbers.

E.g.8 Determine the two integers between which the irrational number  $\sqrt{7}$  lies.

\*\*\*\*\*

Choose the two perfect squares on either side of 7:

$$\sqrt{4} < \sqrt{7} < \sqrt{9}$$

$$\therefore 2 < \sqrt{7} < 3$$

Exercise 8: Date:

- (1) Which of the numbers are Rational numbers ( $\mathbb{Q}$ ) and which are Irrational numbers ( $\mathbb{Q}'$ )?
  - (a) 14 : \_\_\_\_ (b)  $\frac{1}{5}$  : \_\_\_\_ (c)  $\sqrt{81}$  : \_\_\_\_
  - (d) 0,12 : \_\_\_\_ (e)  $\sqrt{18}$  : \_\_\_\_ (f) 12, $\dot{2}\dot{3}$  : \_\_\_\_
- (g)  $-\sqrt{\frac{12}{3}}$  : \_\_\_\_\_ (h) 0,2945 ... : \_\_\_\_\_ (i)  $\sqrt[3]{64}$  : \_\_\_\_\_
- (j)  $\pi$  : \_\_\_\_ (k)  $\sqrt[5]{32}$  : \_\_\_\_ (l)  $\frac{11}{7}$  : \_\_\_\_

	_						
(2)	Between	which two	integers	do the	following	irrational	numbers lie?

(a)  $-\sqrt{12}$ 

(b)  $\sqrt{66}$ 

\_\_\_\_

\_\_\_\_

(c)  $\sqrt[3]{5}$ 

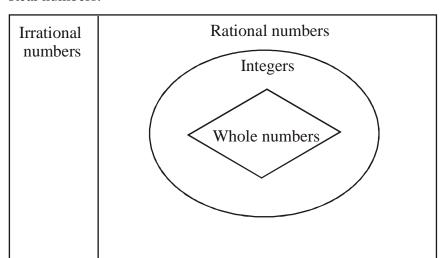
(d)  $\sqrt[5]{2}$ 

\_\_\_\_

(3) The diagram below is a summary of all the numbers that are used on school level. Place the following numbers in the right place on the table; simplify the number if necessary:

$$4\frac{1}{2}$$
 ;  $\sqrt[3]{8}$  ;  $\sqrt{8}$  ;  $-16$  ; 0,45 ; 0,3 ;  $\frac{18}{6}$  ; 0,2387 ... ;  $\frac{0}{17}$  ; 6,88

Real numbers:



② (1) Except for the real numbers we also have the non-real numbers. Give an example of a non-real number.

(2) What is the set called that contain all real and non-real numbers?

\_\_\_\_\_

#### **A1.4** Representation of sets of numbers:

Sets of numbers can be represented or written in the following ways:

#### A1.4.1 Set builder notation:

E.g. 9 Write the following sets of numbers in set builder notation:

- (a) All natural numbers greater than 6:  $\{x / x > 6; x \in \mathbb{N} \}$
- (b) All real numbers between -2 and 5:  $\{m: -2 < m < 5 ; m \in \mathbb{R}\}$

#### A1.4.2 <u>Interval notation</u>:

Only sets that form part of real numbers can be represented using interval notation!

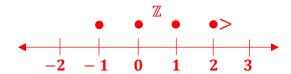
E.g. 10 Write the following in interval notation:

- (a) The real numbers between -2 and 4, including 4:  $x \in (-2; 4]$  Open, closed interval!
- (b)  $\{m \mid m > 7; m \in \mathbb{R}\}$ :  $m \in (7; \infty)$  Open interval!

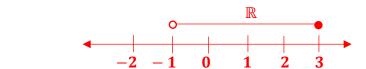
#### A1.4.3 Number lines:

E.g. 11 Represent the following on a number line:

(a) 
$$\{-1; 0; 1; 2; \dots \dots \}$$





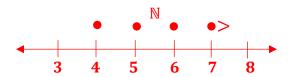


#### A1.4.4 Solving of linear inequalities:

E.g. 12 Solve for x in each of the following and represent the solution on a number line:

(a) 
$$x - 2 \ge 2$$
 if  $x \in \mathbb{N}$   
 $x \ge 2 + 2$   
 $x \ge 4$ 







#### Exercise 9:

Date:		

(1) Write the following in interval notation (if applicable) and represent it on a number line:

(a) 
$$\{x : x < -1; x \in \mathbb{R}\}$$

(b) 
$$\{x : -3 < x < 3; x \in \mathbb{Z}\}$$

(c) 
$$\{y : y < 2; y \in \mathbb{N}\}$$

(d) 
$$\{x : x \ge -3; x \in \mathbb{R}\}$$

(e) 
$$\{x / x < 3; x \in \mathbb{Z}\}$$

(f) 
$$\{p / p \ge \frac{-5}{2}; p \in \mathbb{R}\}$$

(g) 
$$\{m: -2 \le m < 5; m \in \mathbb{R}\}$$

(h) 
$$\{x: x \leq 5; x \in \mathbb{N}_0\}$$

(2) Solve for x in each of the following and represent the solution on a number line:

(a) 
$$x + 1 \le 3; x \in \mathbb{N}_0$$

(b) 
$$2x \ge -8$$
;  $x \in \mathbb{R}$ 

(e) $-6 < x - 1 \le 6; x \in \mathbb{R}$	R	(f) $x + 7 \ge -1$ ; $x \in \mathbb{Z}$
	ractions in its si	Date:implest form: (Without a calculator.)
(1) Convert the following to common f		implest form: (Without a calculator.)
(1) Convert the following to common f		implest form: (Without a calculator.)
5 REVISION EXERCISE:  (1) Convert the following to common f  (a) 14,17		implest form: (Without a calculator.)
(1) Convert the following to common f  (a) 14,17		implest form: (Without a calculator.) (b) 0, 1234

(2) Indicate, by using a  $\checkmark$ , all the rational numbers between 0 and 10:

(a)	(b)	(c)	(d)	(e)	(f)	(g)	(h)	(i)	(j)
$\sqrt{9}$	-1	√8	<u>6</u> 3	<sup>3</sup> √16	π	$\frac{0}{3}$	$\sqrt{144}$	4,124	$\sqrt{\frac{24}{6}}$

_	7,199 (to 1 dec)	-	0,048561 (to 4 dec)	
(c)	234,34 (to 1 dec)	(d)	1 001,1989 (to the near	rest intege
(e)	3,997 (to 2 dec)	(f)	23,712 (to the nearest i	nteger)
_		-		
Plac	ce any two irrational numbers l	between 2 and 3.		
Plac		between 2 and 3.		
Place		petween 2 and 3.		
Bet		e following irrati		
Bet	ce any two irrational numbers l	e following irrati	onal numbers lie?	

(6) Complete the missing representations in the table below:

	Set builder notation:	Interval notation:	Number line:
(a)	$\left\{x/-1 < x \le 2; x \in \mathbb{R}\right\}$		
(b)		$x \in [-2;5]$	
(c)		$y \in (-\infty;3]$	
(d)			$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
(e)	$\{y \mid y \geq 3; y \in \mathbb{N}\}$		
(f)		$m \in (0;4]$	
(g)			-5 -4 -3 -2 -1 0
(h)	$\{m: m \leq 6; m \in \mathbb{R}\}$		
(i)	$\{x / -1 < x < 2; x \in \mathbb{Z}\}$		
(j)		$x \in (-1; \infty)$	

## **Chapter A2**

## **Algebraic expressions**

#### **A2.1 Products:**

#### **A2.1.1** The law of distribution:

E.g. 1 Determine the following products by using the law of distribution:

(a) 
$$(x - 2)(x + 2)$$

(b) 
$$(3m + n)(2m + 5n)$$

(a) x(x + 2) - 2(x + 2) $= x^2 + 2x - 2x - 4$ 

$$= x^{2} + 2x - 2x - 4$$

$$= x^{2} - 4$$

(b) 
$$(3m + 1n)(2m + 5n)$$

 $= 6m^2 + 15mn + 2mn + 5n^2$  $= 6m^2 + 17mn + 5n^2$ 

Exercise 1:

Date: \_\_\_\_\_

Determine the following products:

(1) 
$$(y - 4)(y + 3)$$

(2) 
$$(p-2)(p-7)$$

(2x + 1)(x - 5)(3)

(4) 
$$(x - 2y)(2x - y)$$

(4ab + 1)(2ab - 3)(5)

(6) 
$$(5 - 7m)(2 - 3m)$$

(7) (2a - 4b)(3a + 2b)

(8) 
$$(m+n)(2m-1)$$

(9) (d - 12)(12 + d)

$$(10) \qquad (a^2 + 4)(a^2 + 2)$$


$$(11) \qquad \left(\frac{1}{2}m - 6\right)(8m - 3)$$

$$(12) \qquad (-2k - 5)(5 + 3k)$$

\_\_\_\_\_

$$(13) \qquad \left(p + \frac{1}{p}\right) \left(8p - \frac{4}{p}\right)$$

$$(14) \qquad (abc - 2ac)(abc + 3bc)$$

\_\_\_\_

\_\_\_\_\_

$$(15) \qquad (3r^3 + 2)(2r^2 - 5)$$

(16) 
$$2x(x - 5y)(3x + 2y)$$

\_\_\_\_\_

(17)  $\left(\frac{1}{p^3q^2} - \frac{2}{p^2q}\right)\left(\frac{1}{p} + \frac{2}{q}\right)$  (18)  $\left(\frac{m^2n}{3} - \frac{6}{mn}\right)\left(\frac{mn}{2} - \frac{3}{mn^2}\right)$ 

\_\_\_\_\_

\_\_\_\_\_

#### E.g. 2 Simplify:

(a) 
$$(2a + 1)(2a - 1) = 4a^2 - 2a + 2a - 1 = 4a^2 - 1$$

(b) 
$$(m^2 - 5n)(m^2 + 5n) = m^4 + 5m^2n - 5m^2n - 25n^2 = m^4 - 25n^2$$
  
Or shorter

(c) 
$$(xy + 3)(xy - 3) = x^2y^2 - 9$$

(d) 
$$\left(\frac{ab}{4} - \frac{1}{7}\right) \left(\frac{ab}{4} + \frac{1}{7}\right) = \frac{a^2b^2}{16} - \frac{1}{49}$$

_	_	
-		

Exercise 2:

Date: \_\_\_\_\_

Simplify:

(1) 
$$(abc - 2)(abc + 2)$$

$$(2) \qquad \left(\frac{1}{3} + 5t\right)\left(\frac{1}{3} - 5t\right)$$

(3) 
$$(p - 9q)(9q + p)$$

(4) 
$$(n + 7k)(7n - k)$$

 $(5) \qquad (-a + 4b)(-a - 4b)$ 

(6) 
$$-x\left(\frac{1}{x}-x\right)\left(\frac{1}{x}+x\right)$$

$$(7) \qquad (x^{2m} - 8)(x^{2m} + 8)$$

$$(8) \qquad (0,3 + 3q)(0,3 - 3q)$$

(9) 
$$(b^6c^3 + 6)(b^6c^3 + 6)$$

$$(10) \qquad (4xk^5 - 7)(7 + 4xk^5)$$

$$(11) (m - 2n)^2(m + 2n)^2$$

$$(12) \qquad \left(\frac{m}{n} + 2\right) \left(\frac{m^2}{n^2} + 4\right) \left(\frac{m}{n} - 2\right)$$

\_\_\_\_\_

#### A2.1.2 **Squaring of a binomial:**

#### E.g. 3 Determine the following products:

(a) 
$$(2x + 1)^2$$

\*\*\*\*\*

$$= (2x + 1)(2x + 1)$$

$$= 4x^{2} + 2x + 2x + 1$$

$$= 4x^{2} + 4x + 1$$

(b) 
$$\left(m - \frac{1}{m}\right)^2$$

$$= \left(m - \frac{1}{m}\right)\left(m - \frac{1}{m}\right)$$

$$= m^2 - \frac{m}{m} - \frac{m}{m} + \frac{1}{m^2}$$

$$= m^2 - 2 + \frac{1}{m^2}$$

#### Exercise 3:

Date: \_\_\_\_\_

Determine the following squares:

(1) 
$$(y - 11)^2$$

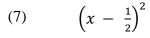
(2) 
$$(3p + 2q)^2$$

$$(3) \qquad (-4 + 5c)^2$$

$$(4) \qquad (mn+3)^2$$

$$(5) (k^2 + 1)^2$$

 $(8 - 3b)^2$ (6)



 $\left(\frac{y}{5}-3\right)^2$ (8)

$$(9) (5p - 2p^2)^2$$

$$(10) \qquad \left(4 + \frac{3}{n}\right)^2$$

\_\_\_\_\_

\_\_\_\_\_

$$(11) \qquad (0.2 + 6y)^2$$

$$(12) \qquad \left(\frac{2m}{p} + \frac{p^2}{3m}\right)^2$$

\_\_\_\_

\_\_\_\_

E.g. 4 Simplify the following: (Shorter method!)

(a) 
$$(m + 5n)^2 = (m)^2 + 2(m)(5n) + (5n)^2 = m^2 + 10mn + 25n^2$$

(b) 
$$(pq - 2)^2 = p^2q^2 - 4pq + 4$$

(c) 
$$\left(\frac{1}{3} + 3x\right)^2 = \frac{1}{9} + 2x + 9x^2$$

Exercise 4: Date:

Simplify (Use the shorter method!)

$$(1) (x - 3)^2$$

(2) 
$$(6m - 1)^2$$

$$(3) \qquad (3y + 7)^2$$

$$(4) \qquad (3 + pq)^2$$

$$(5) \qquad (5t^2 + 8)^2$$

$$(6) \qquad \left(\frac{2}{3} - 6y\right)^2$$

$$(7) \qquad (-2k - 5)^2$$

$$(8) \qquad \left(\frac{3p-2q}{5m}\right)^2$$

\_\_\_\_\_

$$(9) \qquad (4x^2 + 10 y^2)^2$$

$$(10) \qquad (2mn + 7)(7 + 2mn)$$

(11)	(5	2 _	3 <i>y</i> )	(Ω	ㅗ	211
(11)	()	<b>5</b> —	<i>57</i> ()	(Ö	+	3 y

$$(12) -2(abc - 11)^2$$

#### **A2.1.3** Binomials and trinomials:

E.g. 5 Simplify the following products:

$$(4y + 1)(y^{2} - y + 5)$$

$$= 4y^{3} - 4y^{2} + 20y + 1y^{2} - 1y + 5$$

$$= 4y^{3} - 3y^{2} + 19y + 5$$

Exercise 5:

Date: \_\_\_\_\_

Simplify the following products:

(1) 
$$(2a - 3)(a^2 + 5a - 4)$$

$$(2) \qquad (m+7)(2m^2+3m+3)$$

$$(3) \qquad (1+x)(1-x+x^2)$$

$$(4) \qquad (3y - 2)(9y^2 + 6y + 4)$$

(5)  $\left(2m + \frac{1}{2}\right)\left(\frac{m^2}{4} + 4 - 4m\right)$ 

(6) 
$$(m^2n^2 - 5)(25 + 5m^2n^2 + m^4n^4)$$

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#### A2.1.4 The sum and difference of two cubes:

#### E.g. 6 Consider the following:

**Product:** 

(a) 
$$(x - 3)(x^2 + 3x \oplus 9) = x^3 + 3x^2 + 9x - 3x^2 - 9x - 27 = x^3 - 27$$

(b) 
$$(y + 5)(y^2 - 5y + 25) = y^3 - 5y^2 + 25y + 5y^2 - 25y + 125 = y^3 + 125$$
Pattern:

Pattern:  
(c) 
$$(4m-1)(16m^2+4m+1) = (4m-1)[(4m)^2+(4m)(1)+(1)^2] = 64m^3-1$$
  
Pattern:  
(d)  $(n^2+2)(n^4-2n^2+4) = (n^2+2)[(n^2)^2-(2)(n^2)+(2)^2] = n^6+8$ 

(d) 
$$(n^2 + 2)(n^4 - 2n^2 + 4) = (n^2 + 2)[(n^2)^2 - (2)(n^2) + (2)^2] = n^6 + 8$$

#### Exercise 6: Date:

Write down the following products directly, if possible:

(1) 
$$(a + 3)(a^2 - 3a + 9)$$

$$(2) \qquad (2y^3 + 4)(4y^6 - 8y^3 + 16)$$

(3) 
$$\left(\frac{x}{3}-1\right)\left(\frac{1}{9}x^2+\frac{1}{3}x+1\right)$$

(4) 
$$\left(6a^2 - \frac{1}{2}\right)\left(36a^4 + 3a^2 + \frac{1}{4}\right)$$

$$(5) \qquad (5q + 7)(25q^2 - 35q + 49)$$

(6) 
$$(8 - 3m)(9m^2 + 24m + 64)$$

 $(x - 5)(x^2 - 5x + 25)$ (7)

(8) 
$$(0.1 + 0.2y)(0.01 - 0.02y + 0.04y^2)$$

 $(9a^4 + 6a^2b + 4b^2)(3a^2 - 2b)$ (9)

$$(10) 2(-1 + 5m)(25m^2 + 5m + 1)$$